Time Series Analysis and Inverse Theory for Geophysicists

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TIME SERIES ANALYSIS AND INVERSE THEORY FOR GEOPHYSICISTS

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Contents

	Prefa	ice	pag	ze xi
	Ackn	owledgements		xiii
	List o	of illustrations		xiv
1	Introduction			1
	1.1	The digital revolution		1
	1.2	Digital recording		3
	1.3	Processing		5
	1.4	Inversion		7
	1.5	About this book		10
		Exercises		12
Pa	rt I P	rocessing		15
2	Mathematical preliminaries: the z- and discrete Fourier transforms			17
	2.1	The z-transform		17
	2.2	The discrete Fourier transform		21
	2.3	2.3 Properties of the discrete Fourier transform		
	2.4	DFT of random sequences		34
		Exercises		36
3	Practical estimation of spectra			40
	3.1	Aliasing		40
	3.2	Spectral leakage and tapering		44
	3.3	Examples of spectra		49
		Exercises		53
4	Processing of time sequences			57
	4.1	Filtering		57
	4.2	Correlation		63
	4.3	Deconvolution		65
		Exercises		69

viii		Contents				
5	Proce	essing two-dimensional data		73		
	5.1	The 2D Fourier transform		73		
	5.2	2D filtering		75		
	5.3	Travelling waves		77		
		Exercises		80		
Par	Part II Inversion					
6	Linea	ar parameter estimation		85		
	6.1	The linear problem		85		
	6.2	Least-squares solution of over-determined problems		89		
	6.3	Weighting the data		92		
	6.4	Model covariance matrix and the error ellipsoid		100		
	6.5	Robust methods		103		
		Exercises		107		
7	The	under-determined problem		110		
	7.1	The null space		110		
	7.2	The minimum-norm solution		112		
	7.3	Ranking and winnowing		113		
	7.4	Damping and the trade-off curve		115		
	7.5	Parameter covariance matrix		117		
	7.6	The resolution matrix		121		
		Exercises		123		
8	Nonl	inear inverse problems		125		
	8.1	Methods available for nonlinear problems		125		
	8.2	Earthquake location: an example of nonlinear parameter				
		estimation		127		
	8.3	Quasi-linearisation and iteration for the general problem		130		
	8.4	Damping, step-length damping, and covariance and				
		resolution matrices		131		
	8.5	The error surface		132		
		Exercises		135		
9	Cont	inuous inverse theory		138		
	9.1	A linear continuous inverse problem		138		
	9.2	The Dirichlet condition		139		
	9.3	Spread, error and the trade-off curve		142		
	9.4	Designing the averaging function		144		
	9.5	Minimum-norm solution		145		
	9.6	Discretising the continuous inverse problem		147		
	9.7	Parameter estimation: the methods of Backus and Parker		149		
		Exercises		154		

Contents

Par	t III	Application	15	157	
10	Fourier analysis as an inverse problem				
	10.1	10.1 The discrete Fourier transform and filtering			
	10.2	Wiener filt	ers	161	
	10.3	Multi-tape	r spectral analysis	164	
11	Seismic travel times and tomography			170	
	11.1 Beamforming				
	11.2	Tomograph	hy	177	
	11.3 Simultaneous inversion for structure and earthquake location				
12	Geomagnetism			188	
	12.1	Introductio	on	188	
	12.2	The forward	rd problem	189	
	12.3 The inverse problem: uniqueness			190	
	12.4 Damping			193	
	12.5 The data			196	
	12.6 Solutions along the trade-off curve			199	
	12.7	12.7 Covariance, resolution and averaging functions			
	12.8	12.8 Finding fluid motion in the core			
	Appe	ndix 1 Fou	urier series	213	
	Appe	ndix 2 The	e Fourier integral transform	218	
	Appendix 3 Shannon's sampling theorem		224		
	Appendix 4 Linear algebra		226		
	Appe	ndix 5 Veo	ctor spaces and the function space	234	
	Appe	ndix 6 Lag	grange multipliers and penalty parameters	241	
	Appendix 7 Files for the computer exercises		244		
	Refer	ences		246	
	Index			250	

ix